Saturation: Recent Developments, New Ideas and Measurements

Andrey Tarasov



Synergies of pp and pA Collisions with an Electron-Ion Collider RIKEN BNL Research Center Workshop June 26-28, 2017 at Brookhaven National Laboratory

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Volume 129



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- TMD physics
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- · Particle production in pA
- Correlations

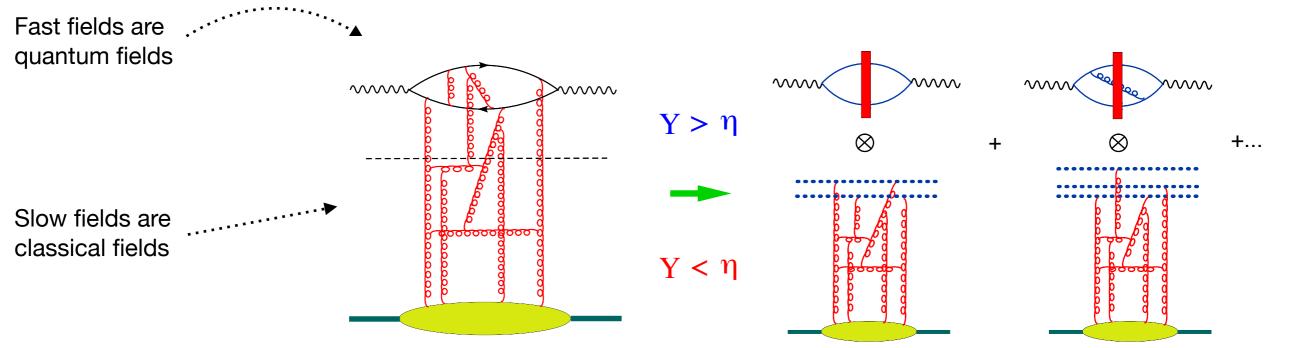
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Rapidity factorization of high-energy scattering processes at NLO

Rapidity factorization approach



I. Balitsky, G.A. Chirilli

$$\begin{split} T\{\hat{j}_{\mu}(x)\hat{j}_{\nu}(y)\} &= \int d^{2}z_{1}d^{2}z_{2} \ I^{\text{LO}}_{\mu\nu}(z_{1},z_{2},x,y) \text{tr}[\{\hat{U}^{\eta}_{z_{1}}\hat{U}^{\dagger\eta}_{z_{2}}\}]^{\text{conf}} \\ &+ \int d^{2}z_{1}d^{2}z_{2}d^{2}z_{3} \ I^{\text{NLO}}_{\mu\nu}(z_{1},z_{2},z_{3},x,y) [\frac{1}{N_{c}} \text{tr}\{\hat{U}^{\eta}_{z_{1}}\hat{U}^{\dagger\eta}_{z_{3}}\} \text{tr}\{\hat{U}^{\eta}_{z_{3}}\hat{U}^{\dagger\eta}_{z_{2}}\} - \text{tr}\{\hat{U}^{\eta}_{z_{1}}\hat{U}^{\dagger\eta}_{z_{2}}\}] \\ & \qquad \qquad \qquad \\ & \qquad \qquad \qquad \\ & \qquad \qquad \\ & \qquad \qquad \\ & \qquad \qquad \qquad \\$$

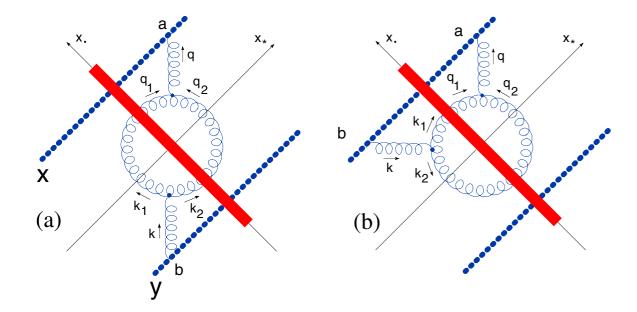
Giovanni Antonio Chirilli

Rapidity factorization of high-energy scattering processes at NLO

NLO evolution of conformal dipoles in QCD

$$\begin{split} &2a\frac{d}{da}[\operatorname{tr}\{\hat{U}_{z_{1}}U_{z_{2}}^{\dagger}\}]^{\operatorname{conf}} \ = \ \frac{\alpha_{s}}{2\pi^{2}}\int\!d^{2}z_{3} \, \left([\operatorname{tr}\{\hat{U}_{z_{1}}\hat{U}_{z_{3}}^{\dagger}\}\operatorname{tr}\{\hat{U}_{z_{3}}\hat{U}_{z_{2}}^{\dagger}\} - N_{c}\operatorname{tr}\{\hat{U}_{z_{1}}\hat{U}_{z_{2}}^{\dagger}\}]^{\operatorname{conf}} \\ &\times \frac{z_{12}^{2}}{z_{13}^{2}z_{23}^{2}} \left[1 + \frac{\alpha_{s}N_{c}}{4\pi} \left(b \ln z_{12}^{2}\mu^{2} + b \frac{z_{13}^{2} - z_{23}^{2}}{z_{13}^{2}z_{23}^{2}} \ln \frac{z_{13}^{2}}{z_{23}^{2}} + \frac{67}{9} - \frac{\pi^{2}}{3}\right)\right] \\ &+ \frac{\alpha_{s}}{4\pi^{2}} \int \frac{d^{2}z_{4}}{z_{34}^{4}} \left\{\left[-2 + \frac{z_{14}^{2}z_{23}^{2} + z_{24}^{2}z_{13}^{2} - 4z_{12}^{2}z_{34}^{2}}{2(z_{14}^{2}z_{23}^{2} - z_{24}^{2}z_{13}^{2})} \ln \frac{z_{14}^{2}z_{23}^{2}}{z_{24}^{2}z_{23}^{2}}\right] \\ &\times \left[\operatorname{tr}\{\hat{U}_{z_{1}}\hat{U}_{z_{3}}^{\dagger}\}\operatorname{tr}\{\hat{U}_{z_{3}}\hat{U}_{z_{4}}^{\dagger}\}\{\hat{U}_{z_{4}}\hat{U}_{z_{2}}^{\dagger}\} - \operatorname{tr}\{\hat{U}_{z_{1}}\hat{U}_{z_{3}}^{\dagger}\hat{U}_{z_{4}}\hat{U}_{z_{2}}^{\dagger}\hat{U}_{z_{3}}\hat{U}_{z_{4}}^{\dagger}\} - (z_{4} \to z_{3})\right] \\ &+ \frac{z_{12}^{2}z_{34}^{2}}{z_{13}^{2}z_{24}^{2}} \left[2\ln \frac{z_{12}^{2}z_{34}^{2}}{z_{14}^{2}z_{23}^{2}} + \left(1 + \frac{z_{12}^{2}z_{34}^{2}}{z_{13}^{2}z_{24}^{2} - z_{14}^{2}z_{23}^{2}}\right) \ln \frac{z_{13}^{2}z_{24}^{2}}{z_{14}^{2}z_{23}^{2}}\right] \\ &\times \left[\operatorname{tr}\{\hat{U}_{z_{1}}\hat{U}_{z_{3}}^{\dagger}\}\operatorname{tr}\{\hat{U}_{z_{3}}\hat{U}_{z_{4}}^{\dagger}\}\operatorname{tr}\{\hat{U}_{z_{4}}\hat{U}_{z_{4}}^{\dagger}\} - \operatorname{tr}\{\hat{U}_{z_{1}}\hat{U}_{z_{4}^{\dagger}}\hat{U}_{z_{3}}\hat{U}_{z_{4}}^{\dagger}\hat{U}_{z_{3}}\hat{U}_{z_{4}^{\dagger}}^{\dagger}\} - (z_{4} \to z_{3})\right]\right\} \end{split}$$

I. Balitsky, G.A. Chirilli



This result was obtained in rapidity factorization approach

What about other operators?

Michael Lublinsky

From light-cone wave function to NLO JIMWLK

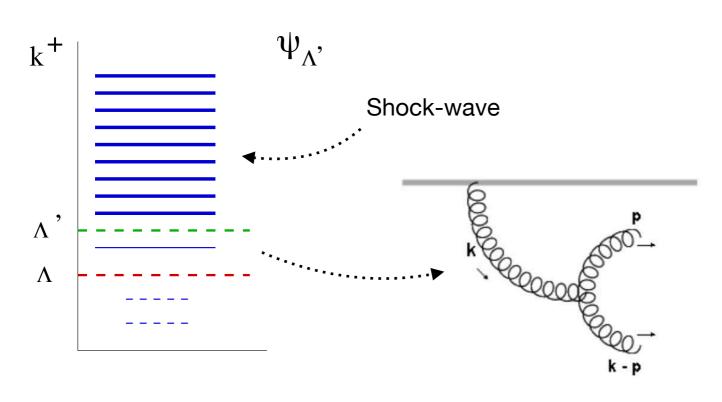
Presented new results on calculation of H at NLO order

The result can be used for any operator

$$\partial_{Y}\left[S^{ab}(x)\right] = -H^{NLO\,JIMWLK}\left[S^{ab}(x)\right]$$

$$\partial_{Y}\left[S^{ab}(x)S^{cd}(y)\right] = -H^{NLO\,JIMWLK}\left[S^{ab}(x)S^{cd}(y)\right]$$

$$\partial_{Y}\left[S^{ab}(x)S^{cd}(y)S^{ef}(z)\right] = -H^{NLO\,JIMWLK}\left[S^{ab}(x)S^{cd}(y)S^{ef}(z)\right]$$



The form of the operator was first obtained by comparison with other results

A. Kovner, M. Lublinsky, Y. Mulian

$$egin{aligned} \ket{\Psi_{
m NLO}} &= \mathcal{N}\ket{0} + \sum_{
m i}\ket{
m i} \left[-rac{ra{
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m k}ra{
m k}\ket{
m H_{
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m E_{
m i}\,{
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m E_{
m k}}} \end{array}$$

Guillaume Beuf

Full NLO corrections for DIS structure functions in the dipole factorization formalism

Now the evolution at NLO is known. What about observables?

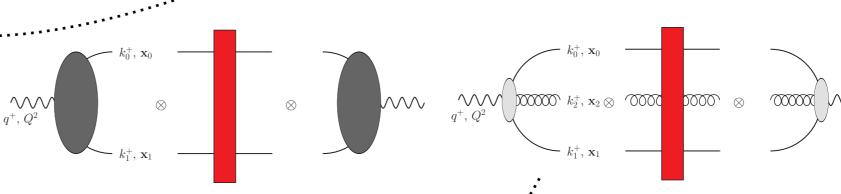
Calculated LF wave function

 $\sigma_{\lambda}^{\gamma} = 2N_{c} \sum_{q_{0}\bar{q}_{1} \text{ F. states}} \frac{2\pi\delta(k_{0}^{+} + k_{1}^{+} - q^{+})}{2q^{+}} \left| \widetilde{\psi}_{\gamma_{\lambda} \to q_{0}\bar{q}_{1}} \right|^{2} \operatorname{Re} \left[1 - S_{01} \right] + 2N_{c} C_{F} \sum_{q_{0}\bar{q}_{1}g_{2} \text{ F. states}} \frac{2\pi\delta(k_{0}^{+} + k_{1}^{+} + k_{2}^{+} - q^{+})}{2q^{+}}$

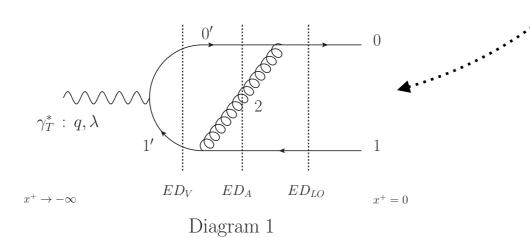
 $\times \left| \widetilde{\psi}_{\gamma_{\lambda} \to q_{0} \bar{q}_{1} g_{2}} \right|^{2} \operatorname{Re} \left[1 - \mathcal{S}_{012}^{(3)} \right] + \cdots$

Demanding calculation with cumbersome expressions

Showed cancellation of UV divergencies



Typical diagram



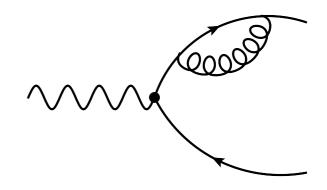
Explicit dependence on the cut-off parameter

Risto Paatelainen

Towards higher-order accuracy in LCPT

LCPT calculations in CGC slowly approaching the NLO level. Perturbative computation of wave functions is quite tedious (hard to automatize)

Introduce a new helicity formulation for LCPT. Perturbative (NLO) computation of wave functions is easy and can be fully automatized



One should take care of UV divergencies. Applied new Four Dimensional Helicity (FDH) scheme (T. Lappi & R. Paatelainen)

$$\begin{aligned} \psi_{\text{(full)}}^{\gamma_{\text{T}}^* \to q\bar{q}} \bigg|_{\text{FDH}} &= \psi_{\text{LO}}^{\gamma_{\text{T}}^* \to q\bar{q}}(\mathbf{p}, z) \left(\frac{g_{\text{R}}^2 C_{\text{F}}}{8\pi^2} \right) \left\{ \left[\frac{3}{2} + \log\left(\frac{\alpha}{z}\right) + \log\left(\frac{\alpha}{1-z}\right) \right] C_{\text{full}} \right. \\ &+ \frac{1}{2} \log^2\left(\frac{z}{1-z}\right) - \frac{\pi^2}{3} + \frac{5}{2} - \log(z(1-z)) \right\} + \left(\frac{g_{\text{R}}^2 C_{\text{F}}}{8\pi^2} \right) \times \Pi + \mathcal{O}(\varepsilon) \end{aligned}$$

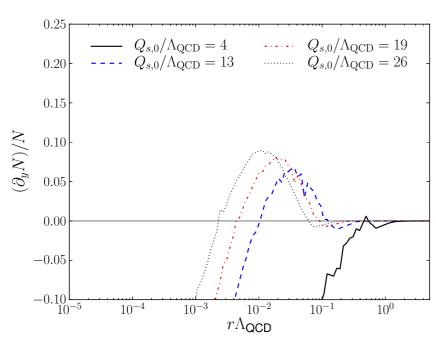
Results from two different schemes

$$\psi_{\text{(full)}}^{\gamma_{\text{T}}^* \to q\bar{q}} \Big|_{\text{CDR}} = \psi_{\text{LO}}^{\gamma_{\text{T}}^* \to q\bar{q}}(\mathbf{p}, z) \left(\frac{g_{\text{R}}^2 C_{\text{F}}}{8\pi^2} \right) \left\{ \left[\frac{3}{2} + \log\left(\frac{\alpha}{z}\right) + \log\left(\frac{\alpha}{1-z}\right) \right] C_{\text{full}} \right. \\
\left. + \frac{1}{2} \log^2\left(\frac{z}{1-z}\right) - \frac{\pi^2}{3} + \frac{5}{2} + \frac{1}{2} \right\} + \mathcal{O}(\varepsilon)$$

Edmond Iancu

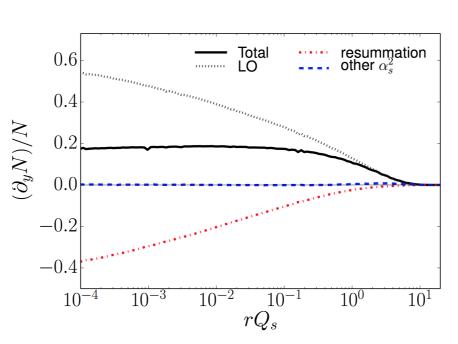
Particle production in pA collisions beyond leading order

"Negative growth" of the dipole scattering amplitude



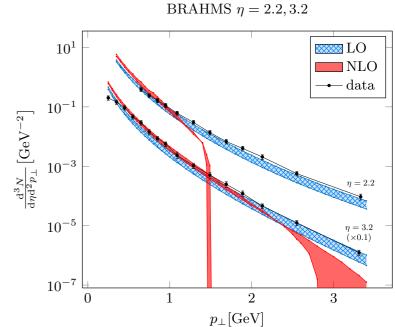
Lappi, Mäntysaari, arXiv:1502.02400

Collinear improvement of NLO BK



Lappi, Mäntysaari, arXiv:1601.06598

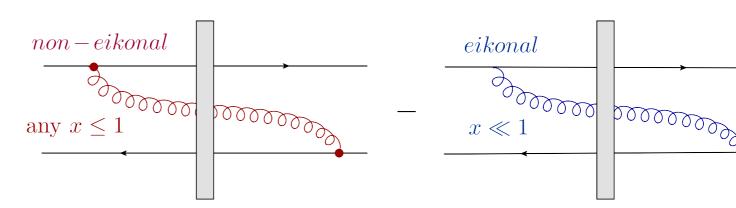
Negative at large p_T



Stasto, Xiao, and Zaslavsky, arXiv:1307.4057

Rapidity subtraction in NLO impact factor

Kang, Vitev, and Xing, arXiv:1403.5221 Altinoluk, Armesto, Beuf, Kovner, and Lublinsky, arXiv:1411.2869 Ducloué, Lappi, and Zhu, arXiv:1604.00225



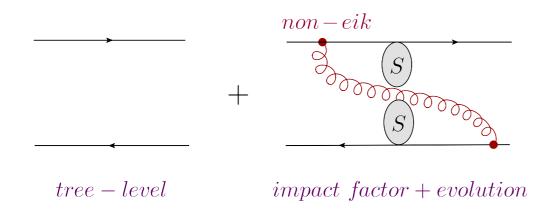
A reorganization of the perturbative expansion which avoids the rapidity subtraction (E.I., A. Mueller and D. Triantafyllopoulos, 2016)

Rapidity subtraction in k_T factorization (G. A. Chirilli, B.-W. Xiao, F. Yuan)

Edmond Iancu

Particle production in pA collisions beyond leading order

The strict separation between a 'LO result' and 'NLO corrections' involves a high degree of fine tuning, leading to instabilities in the presence of seemingly innocuous additional approximations



$$\frac{\mathrm{d}N}{\mathrm{d}\eta\mathrm{d}^{2}\boldsymbol{k}} = \mathcal{S}_{0}(\boldsymbol{k}) + \bar{\alpha}_{s} \int_{X_{a}}^{1} \frac{\mathrm{d}x}{x} \mathcal{K}(\boldsymbol{k};x) \mathcal{S}(\boldsymbol{k},X(x))$$

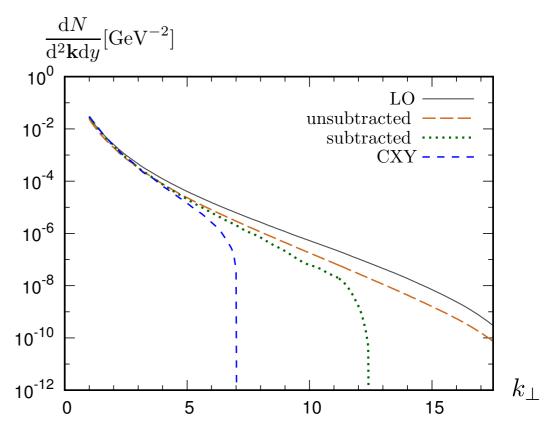
Compute emission with exact kinematics

$$+ \frac{eik}{x} + \frac{non-eik}{s} - \frac{eik}{s}$$

 \mathcal{S} (solution to \mathcal{BK} equation)

 \mathcal{NLO} correction to impact factor

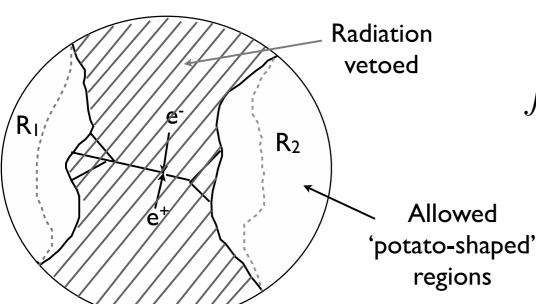
$$\frac{\mathrm{d}N}{\mathrm{d}\eta\mathrm{d}^{2}\boldsymbol{k}} = \mathcal{S}(\boldsymbol{k}, X_{g}) + \bar{\alpha}_{s} \int_{X_{g}}^{1} \frac{\mathrm{d}x}{x} \left[\mathcal{K}(x) - \mathcal{K}(0)\right] \mathcal{S}(\boldsymbol{k}, X(x))$$



Sensible physical results: positive cross-section, but smaller than at LO

Simon Caron-Huot

Linear and non-linear small-x evolution in pQCD

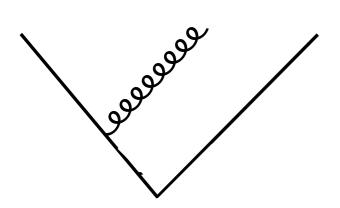


 $\int d\text{Lips}(p_0)|M_3|^2 \to |M_2|^2 \int_{E_0}^Q \frac{dp_0}{p_0} \int \frac{d\Omega}{4\pi} \frac{\alpha_{12}}{\alpha_{10}\alpha_{02}}$

Non-global logarithm

Exploits equivalence with the physics of soft wide-angle radiation, so-called non-global logarithms

Look at this diagram in terms of energy and angular distribution



Presented result on two- and three-loop evolution for non-global logarithms

$$E\frac{d}{dE}U_{12} = \frac{\lambda}{8\pi^2} \int \frac{d^2\Omega_0}{4\pi} \frac{\alpha_{12}}{\alpha_{10}\alpha_{02}} \left(\frac{U_{10}U_{02} - U_{12}}{U_{12}} \right)$$

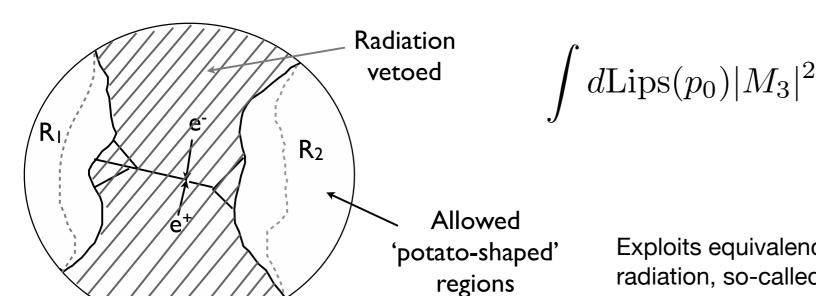


$$\frac{d}{d\eta}U_{12} = \frac{\lambda}{8\pi^2} \int \frac{d^2z_0}{\pi} \frac{z_{12}^2}{z_{10}z_{02}} (U_{10}U_{02} - U_{12})$$

For two loops coincide with the result obtained in rapidity factorization and LCPT approaches

Simon Caron-Huot

Linear and non-linear small-x evolution in pQCD



 $\int d\text{Lips}(p_0)|M_3|^2 \to |M_2|^2 \int_{E_0}^Q \frac{dp_0}{p_0} \int \frac{d\Omega}{4\pi} \frac{\alpha_{12}}{\alpha_{10}\alpha_{02}}$

Non-global logarithm

Exploits equivalence with the physics of soft wide-angle radiation, so-called non-global logarithms

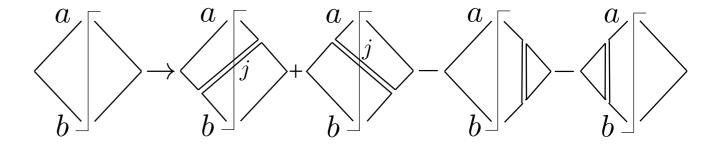
Used duality to construct NLO evolution and NNLO evolution kernel in N = 4 SYM.

$$\begin{split} K^{(2)} &= \int_{i,j,k} \int \frac{d^2 \Omega_0}{4\pi} \frac{d^2 \Omega_{0'}}{4\pi} K^{(2)\ell}_{ijk;00'} i f^{abc} \left(L^a_{i;0} L^b_{j;0'} R^c_k - R^a_{i;0} R^b_{j;0'} L^c_k \right) \\ &+ \int_{i,j} \int \frac{d^2 \Omega_0}{4\pi} \frac{d^2 \Omega_{0'}}{4\pi} K^{(2)N=4,\ell}_{ij;00'} \left(f^{abc} f^{a'b'c'} U^{bb'}_0 U^{cc'}_{0'} - \frac{C_A}{2} (U^{aa'}_0 + U^{aa'}_0) \right) \left(L^a_i R^{a'}_j + R^{a'}_i L^a_j \right) \\ &+ \int_{i,j} \int \frac{d^2 \Omega_0}{4\pi} \frac{\alpha_{ij}}{\alpha_{0i} \alpha_{0j}} \gamma^{(2)}_K \left(R^a_{i;0} L^a_j + L^a_{i;0} R^a_j \right) + K^{(2)N \neq 4} \\ &L^a_{i:0} \equiv \left(L^{a'}_i U^{a'a}_0 - R^a_i \right) \end{split} \tag{3.32}$$

Duff Neil

Finding small-x physics in small-x jets

Non-global logarithms (log. of infra-red energy scale) vs. soft jet factorization theorems



Evolution of color dipoles

· almost BK equation

$$\partial_L g_{ab} = \int_J \frac{d\Omega_j}{4\pi} W_{ab}(j) \left(U_{abj}(L) g_{aj} g_{jb} - g_{ab} \right)$$

$$W_{ab}(j) = \frac{a \cdot b}{a \cdot j j \cdot b}, j = (1, \hat{n}_j)$$

$$U_{abj}(L) = \exp\left(L \int_{S^2/J} \frac{d\Omega_q}{4\pi} W_{aj}(q) + W_{jb}(q) - W_{ab}(q) \right)$$

$$\vdots$$

Resummation of Sudakov effects

Evolution through study of jet substructure

 $U_{abj} \rightarrow 1$.

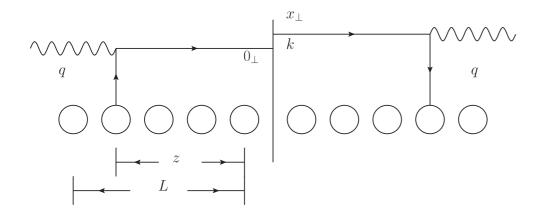
At large values of non-global logarithm L it is possible to simplify it to the BFKL equation

 $\text{duality} \qquad \vdots \qquad \partial_L g_{ab} = \int_{S^2} \frac{d\Omega_j}{4\pi} \frac{a \cdot b}{a \cdot j \, j \cdot b} \Bigg(g_{aj} g_{jb} - g_{ab} \Bigg)$ $\Leftrightarrow \qquad \vdots \qquad \partial_Y S_{\vec{a}\vec{b}} = \frac{\alpha_s C_A}{\pi} \int_{\mathbb{R}^2} \frac{d\Omega_j}{2\pi} \frac{x_{\vec{a}\vec{b}}^2}{x_{\vec{a}\vec{j}}^2 x_{\vec{j}\vec{b}}^2} \Bigg(S_{\vec{a}\vec{j}} S_{\vec{j}\vec{b}} - S_{\vec{a}\vec{b}} \Bigg)$

Al Mueller

Medium induced transverse momentum broadening in hard processes

Transverse momentum broadening of partons in hard processes in the presence of medium.

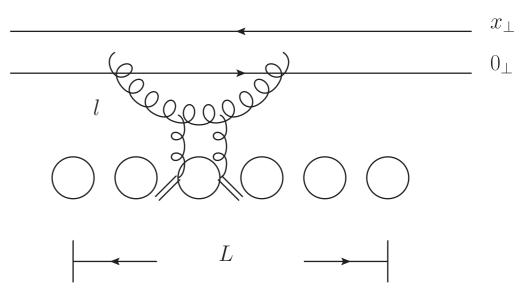


$$\frac{dN}{d^2bd^2k_{\perp}} = \int \frac{d^2x_{\perp}}{(2\pi)^2} e^{-ik_{\perp}\cdot x_{\perp}} \rho x q_N \left(x, \frac{1}{x_{\perp}^2 + 1/Q^2} \right) \times \int_0^L dz e^{-\mathcal{E}},$$

$$\begin{split} \mathcal{E}_{\text{Sud}} &= 2 \frac{\alpha_s C_F}{2\pi} \int_{q_+/[Q^2 x_\perp^2]}^{q_+} \frac{dl_+}{l_+} \int_{1/x_\perp^2}^{\frac{l_+}{q_+}Q^2} \frac{dl_\perp^2}{l_\perp^2} \\ &= \frac{\alpha_s C_F}{2\pi} \ln^2(Q^2 x_\perp^2). \end{split}$$

Factorize the vacuum radiation contribution and medium related P_{T} broadening effects into the Sudakov factor and medium dependent distributions, respectively.





Medium induced radiation

A.H. Mueller, Bin Wu, Bo-Wen Xiao and Feng Yuan, Phys.Rev. D95 (2017), 034007

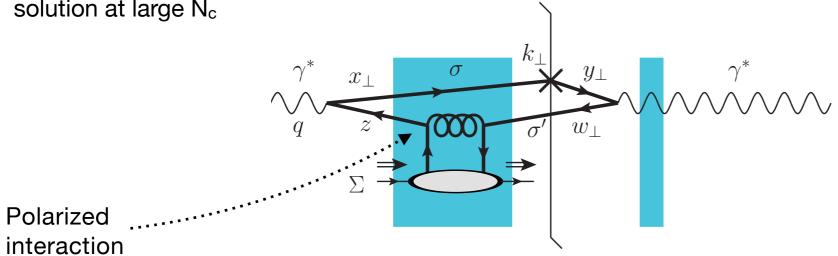
Matthew D. Sievert

Quark helicity evolution at small x

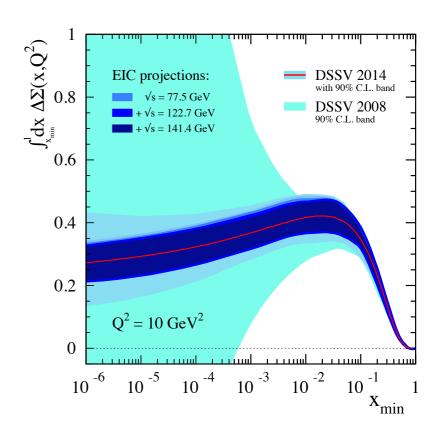
Understanding the proton spin at small x

Small-x helicity evolution (quark helicity TMD & PDF, g₁ structure function)

Numerical and analytic solution at large N_c



E. Aschenaur et al, arXiv:1509.06489



$$g_1^S(x,Q^2) = \frac{N_c N_f}{2\pi^2 \alpha_{EM}} \int_{z_i}^1 \frac{dz}{z^2 (1-z)} \int dx_{01}^2 \left[\frac{1}{2} \sum_{\lambda \sigma \sigma'} |\psi_{\lambda \sigma \sigma'}^T|_{(x_{01}^2,z)}^2 + \sum_{\sigma \sigma'} |\psi_{\sigma \sigma'}^L|_{(x_{01}^2,z)}^2 \right] G(x_{01}^2,z)$$

$$\Delta q^{S}(x,Q^{2}) = \frac{N_{c} N_{f}}{2\pi^{3}} \int_{z_{i}}^{1} \frac{dz}{z} \int_{\frac{1}{z_{s}}}^{\frac{1}{zQ^{2}}} \frac{dx_{01}^{2}}{x_{01}^{2}} G(x_{01}^{2},z)$$

Depend on polarized dipole amplitude

$$x_1 \longrightarrow$$

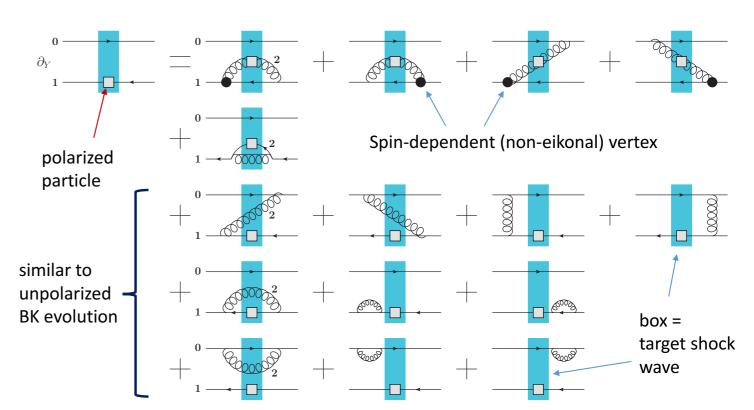
Yuri Kovchegov

Small x asymptotics of the quark helicity distribution

Found evolution equation for polarized dipole

 $\Delta \Sigma^{[x_{min}]}(Q^2)$ 0.5
0.4
0.3
0.2
0.1 10^{-8} 10^{-5} 10^{-2} x_{min}

One can construct an evolution equation for the polarized dipole:



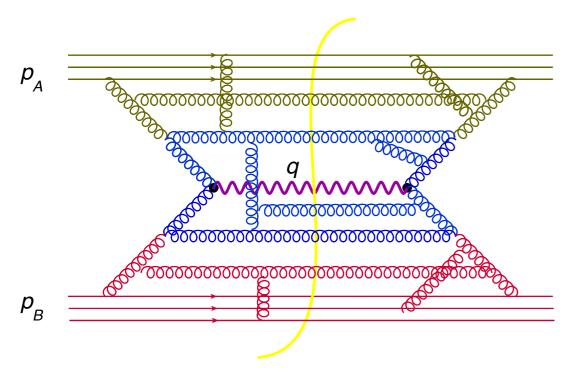
$$G_{10}(z) = G_{10}^{(0)}(z) + \frac{\alpha_s N_c}{2\pi} \int_{z_i}^{z} \frac{dz'}{z'} \int_{\rho'^2}^{x_{10}^2} \frac{dx_{21}^2}{x_{21}^2} \left[2\Gamma_{02,21}(z') S_{21}(z') + 2G_{21}(z') S_{02}(z') + G_{12}(z') S_{02}(z') - \Gamma_{01,21}(z') \right]$$

$$g_1^S(x,Q^2) \sim \Delta q^S(x,Q^2) \sim g_{1L}^S(x,k_T^2) \sim \left(\frac{1}{x}\right)^{\alpha_h} \approx \left(\frac{1}{x}\right)^{2.31} \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

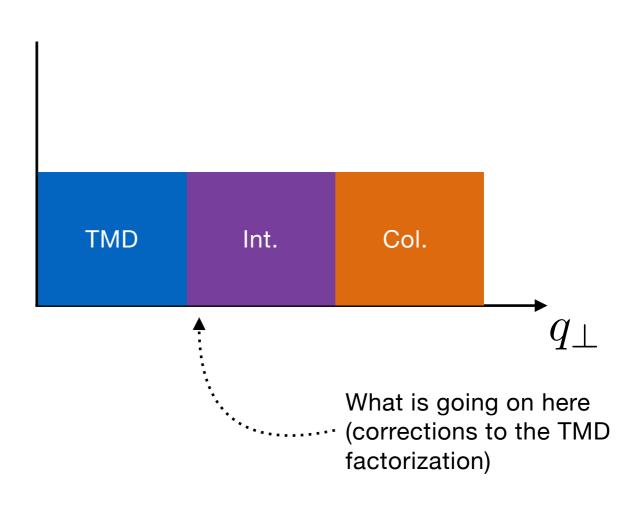
Analytic result:
$$\alpha_h=\frac{4}{\sqrt{3}}\,\sqrt{\frac{\alpha_sN_c}{2\pi}}\,\approx 2.3094\,\sqrt{\frac{\alpha_sN_c}{2\pi}}$$

Ian Balitsky

Higher-twist corrections to gluon TMD factorization



Particle production in pp at small transverse momentum



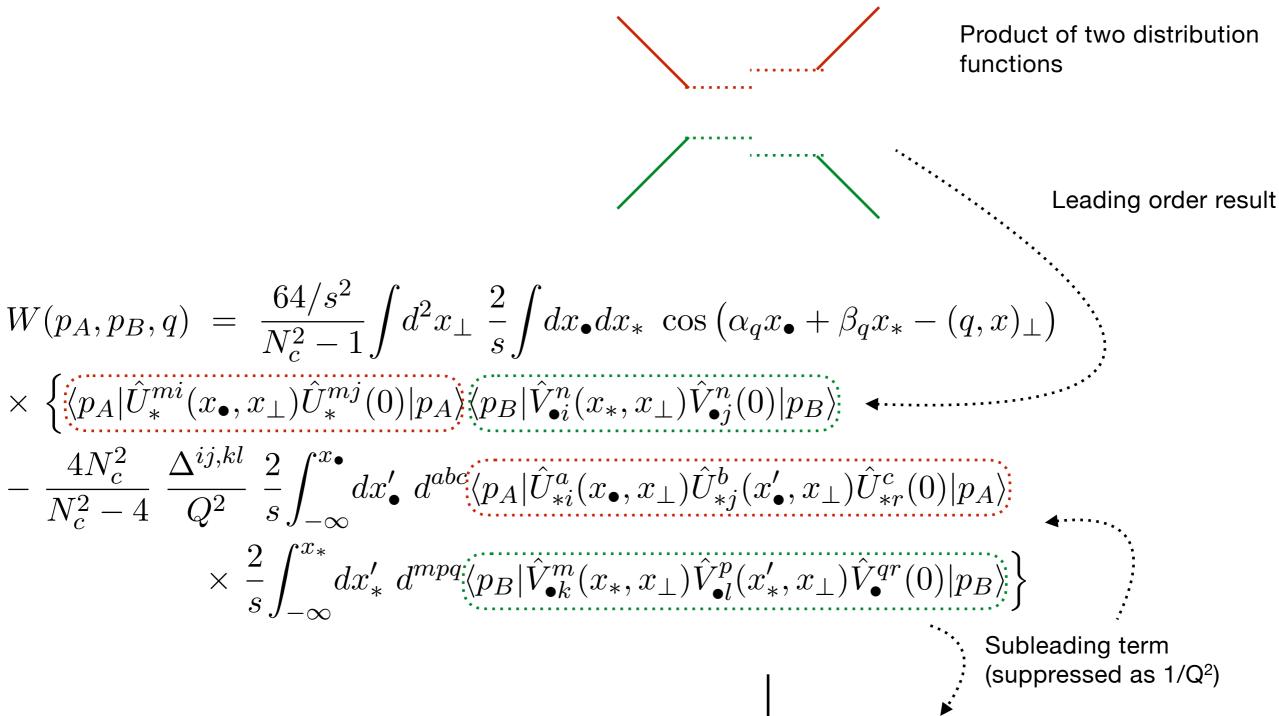
$$\frac{d\sigma}{d\eta d^2 q_{\perp}} = \sum_{f} \int d^2 b_{\perp} e^{i(q,b)_{\perp}} \mathcal{D}_{f/A}(x_A, b_{\perp}, \eta) \mathcal{D}_{f/B}(x_B, b_{\perp}, \eta) \sigma(ff \to H)$$

What is a form of the corrections to this result (Y-term)?

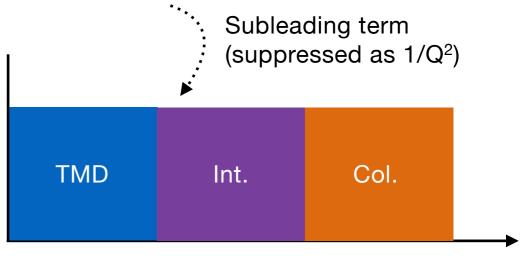
Corrections are suppressed as $\frac{q_{\perp}^2}{Q^2}$

Ian Balitsky

Higher-twist corrections to gluon TMD factorization



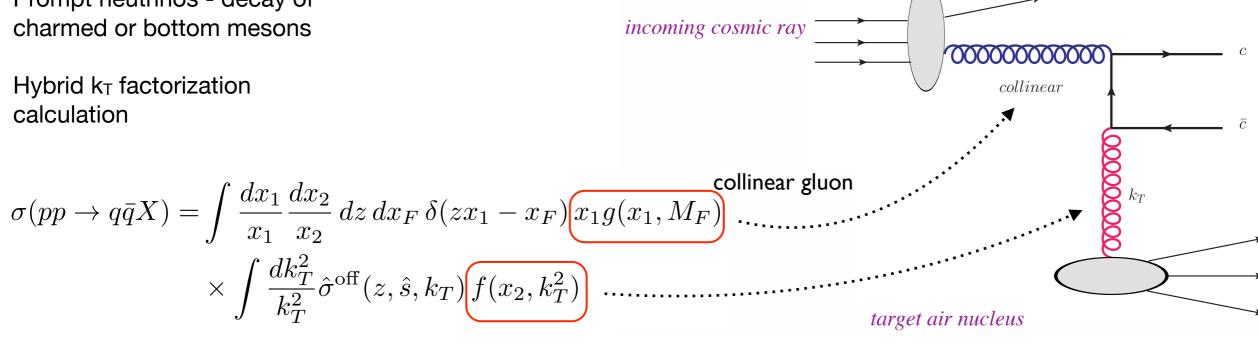
Ian Balitsky, A.T., arXiv:1706.01415



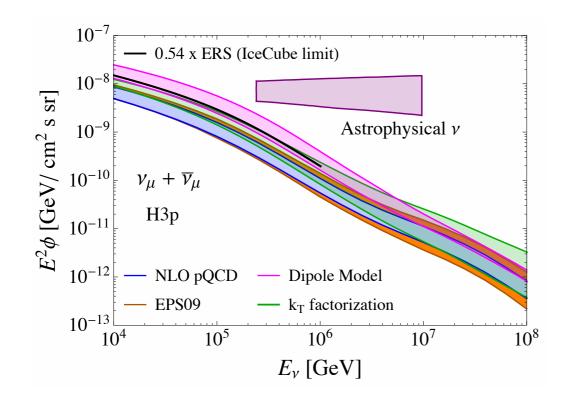
Anna Stasto

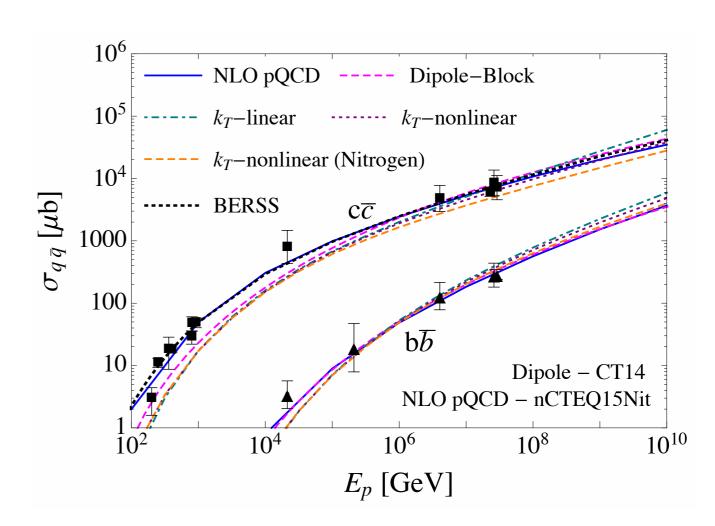
Low x physics and prompt neutrino production

Prompt neutrinos - decay of



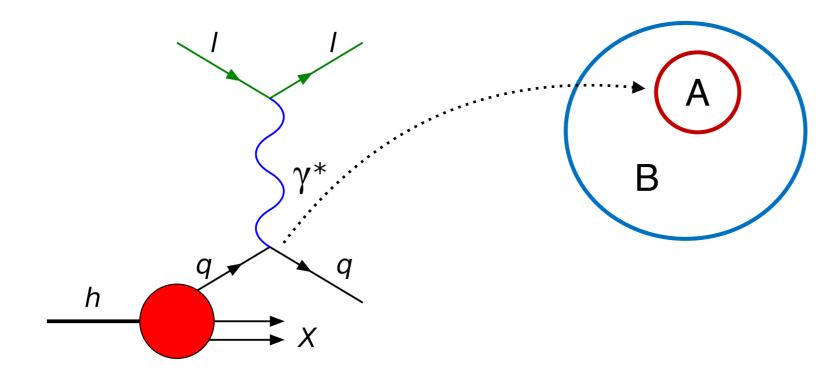
Unintegrated gluon density obtained from the resummed small x evolution equation with non-linear term





Dmitri Kharzeev

Deep Inelastic Scattering as a probe of entanglement



Relation between the entanglement entropy and parton distribution (1D-model)

$$S = \ln[xG(x)]$$

At small-x the entanglement entropy is maximal and the proton is a maximally entangled state

Can extract entanglement entropy from measurements of multiplicity

DIS probes only a part of the proton's wave function (region A)

We sum over all hadronic final states; in quantum mechanics, this corresponds to accessing the density matrix of a mixed state

$$\rho_A = \sum_n \alpha_n^2 |\Psi_n^A\rangle \langle \Psi_n^A|$$

probability of a state with n partons (multiplicity)

 $\alpha_n^2 = p_n$

The entanglement entropy

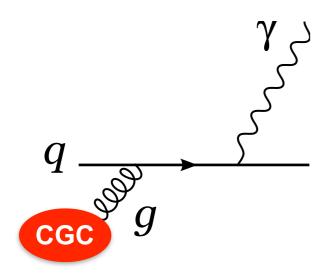
$$S = -\sum_{n} p_n \ln p_n$$

Kenji Fukushima

Particle Production in CGC

Calculation at the NLO level

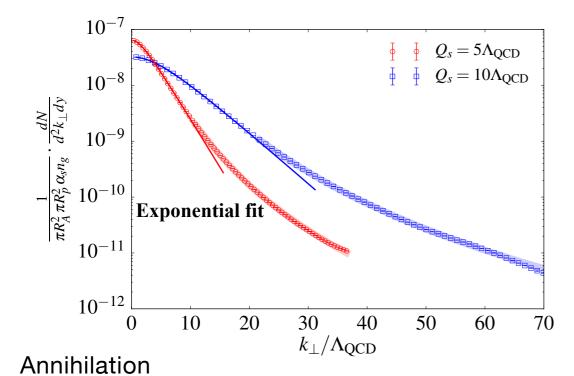
Compton Scattering

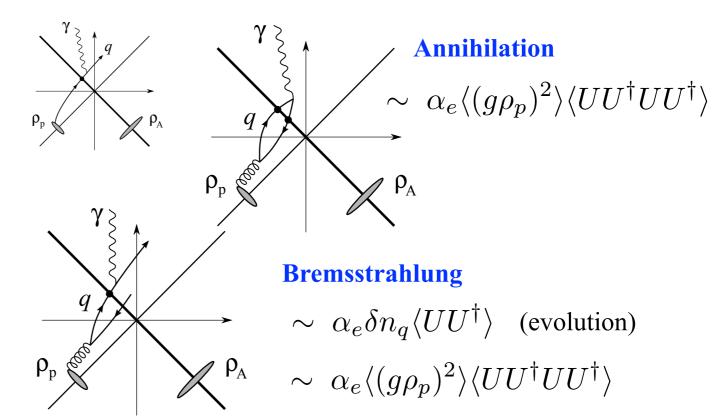


Photons in pA at high energies (LO)

Gelis-Mehtar-Tani (2006)

Benic-Fukushima (2016)





Bremsstrahlung Diagram

PROPERTY OF THE PROPERTY OF TH

Benic-Fukushima-Garcia-Montero-Venugopalan (2016)

$$\mathcal{M}^{\mu}(\boldsymbol{p},\boldsymbol{q},\boldsymbol{k}_{\gamma}) = -q_{f}eg^{2} \int_{\boldsymbol{k}_{\perp},\boldsymbol{k}_{1\perp}} \int_{\boldsymbol{x}_{\perp}\boldsymbol{y}_{\perp}} \frac{\rho_{p}^{a}(\boldsymbol{k}_{1\perp})}{\boldsymbol{k}_{1\perp}^{2}} e^{i\boldsymbol{k}_{\perp}\cdot\boldsymbol{x}_{\perp}+i(\boldsymbol{P}_{\perp}-\boldsymbol{k}_{\perp}-\boldsymbol{k}_{1\perp})\cdot\boldsymbol{y}_{\perp}} \times \bar{u}(\boldsymbol{q}) \left\{ T_{g}^{\mu}(\boldsymbol{k}_{1\perp})U(\boldsymbol{x}_{\perp})^{ba}t^{b} + T_{q\bar{q}}^{\mu}(\boldsymbol{k}_{\perp},\boldsymbol{k}_{1\perp})\tilde{U}(\boldsymbol{x}_{\perp})t^{a}\tilde{U}^{\dagger}(\boldsymbol{y}_{\perp}) \right\} v(\boldsymbol{p})$$

Structure is simple but the full expression is...

Necessary conditions for correctness

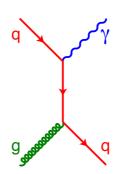
- ✓ Gauge invariance (Coulomb/Light-cone)
- Ward identity: $k_{\gamma\mu}\mathcal{M}^{\mu}(\boldsymbol{p},\boldsymbol{q},\boldsymbol{k}_{\gamma})=0$ satisfied separately for T_g and T_{qq}
- ✓ Leading-twist (perturbative)
- ✓ Soft-photon limit (Low-Burnett-Kroll theorem)

Thomas Peitzmann

Opportunities for Forward Photon Measurements in ALICE at the LHC

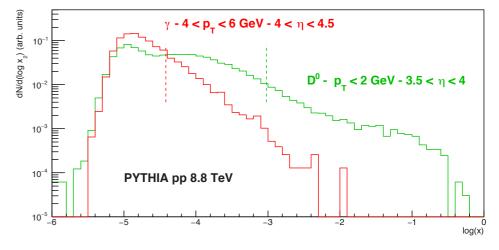
Cleaner observables (EM probes):

- no final state interaction
- well-understood production process
- well-defined kinematics



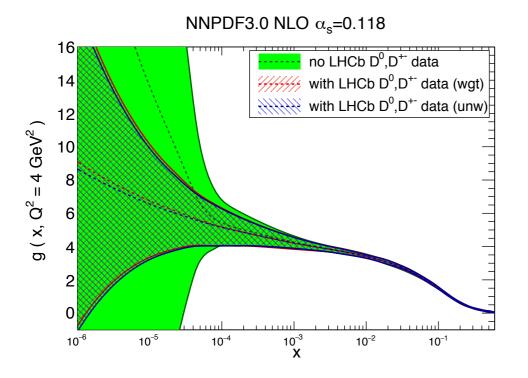
real photons: sensitivity to gluons at LO, clear

kinematic relation



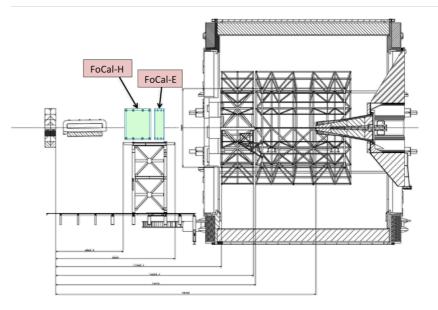
large cross section at small x

- interpretation of hadronic observables remains inconclusive
 - final state modifications in p-A collisions?
 - production process not fully understood for many hadrons
 - · kinematic relation to Bjorken-x uncertain (e.g. fragmentation)
- best alternative candidate: open charm
 - · direct sensitivity to gluons
 - final state interactions?



Usage of forward D measurements by LHCb can constrain gluon distribution





FoCal in ALICE

electromagnetic calorimeter for γ and π^0 measurement

preferred scenario:

at z ≈ 7m (outside magnet)
 3.3 < η < 5.3
 (space to add hadr. calorimeter)

under internal discussion possible installation in LS3

Adrian Dumitru

Fluctuations of the gluon distribution at small-x: correlation of multiplicity and transverse momentum fluctuations

High-energy observable:

$$\langle O[A^+] \rangle = \frac{1}{Z} \int \mathcal{D}A^+ W[A^+] O[A^+] \qquad W[A^+] = e^{-S[A^+]}$$

MV model (no quantum corrections):

$$S[\rho] = \int dx^- d^2x_{\perp} \frac{\operatorname{tr} \rho(x^-, x_{\perp}) \rho(x^-, x_{\perp})}{2\mu^2(x^-)}$$

Proposed new calculation scheme for the functional integral through effective action

$$S_G[\rho] = \int d^2x_{\perp} d^2y_{\perp} \frac{\operatorname{tr} \rho(x_{\perp}) \rho(y_{\perp})}{\mu^2(x_{\perp} - y_{\perp})}$$

E. lancu, K. Itakura and L. McLerran

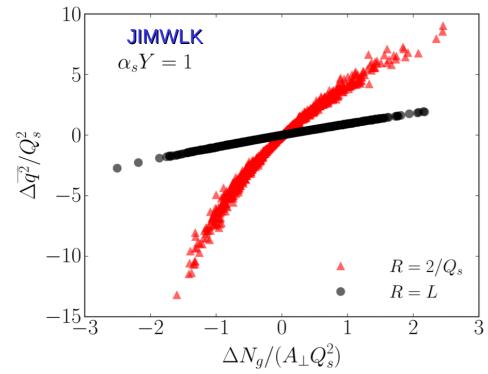
$$e^{-V_{\text{eff}}[X(q)]} = \int \mathcal{D}A^{+}(q) W[A^{+}(q)] \delta(X(q) - O[A^{+}(q)])$$
$$\frac{\delta V_{\text{eff}}[X(k)]}{\delta X(q)} = 0 \to X_{s}(q) \equiv \langle X(q) \rangle$$

Adrian Dumitru, Vladimir Skokov

Adrian Dumitru

Fluctuations of the gluon distribution at small-x: correlation of multiplicity and transverse momentum fluctuations

$$\frac{\delta V_{\rm eff}[X(k)]}{\delta X(q)} = 0 \to X_s(q) \equiv \langle X(q) \rangle$$



Evolution modifies spectrum of fluctuations

Consider fluctuations around this result

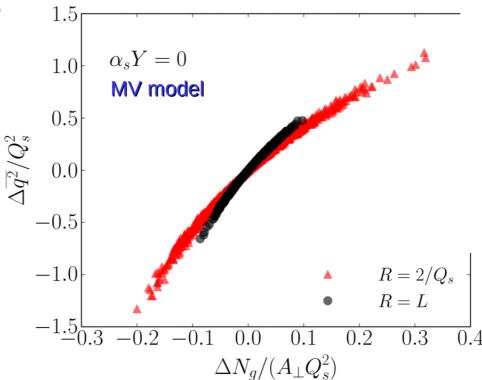
One can understand how this fluctuations affect observables (multiplicity etc.)

$$\Delta \overline{q^2}[\eta(q)] = \frac{\Delta N_g[\eta(q)]}{\int \frac{d^2q}{(2\pi)^2} X_s(q) \eta(q)}$$

$$\Delta N_g \simeq N_c A_{\perp} \Delta \overline{q^2}$$

for small amplitude fluctuations

$$\Delta N_g$$
 increases with $\Delta \overline{q^2}$

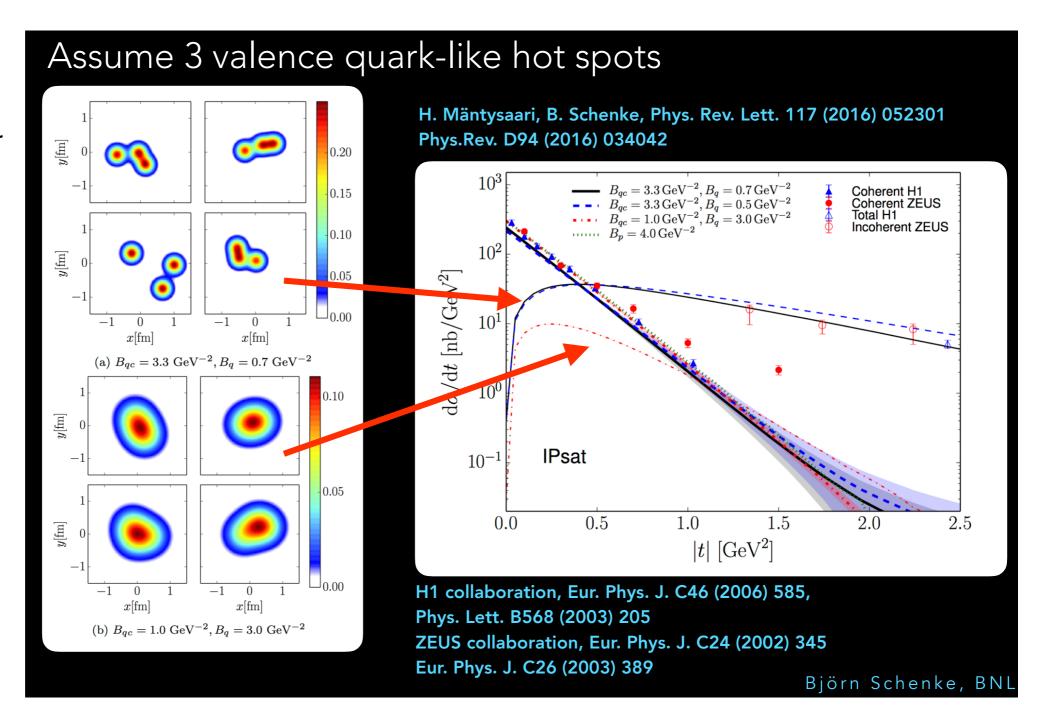


Björn Schenke

Subnucleonic fluctuations, diffraction, and small-x fluctuations

$$\frac{d\sigma^{\gamma^* p \to Vp}}{dt} = \frac{1}{16\pi} \left| \langle \mathcal{A}^{\gamma^* p \to Vp}(x, Q^2, \Delta) \rangle \right|^2$$

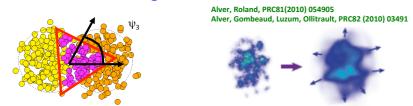
Shape fluctuations of the proton's gluon distribution are needed to describe incoherent diffractive vector meson data from HERA



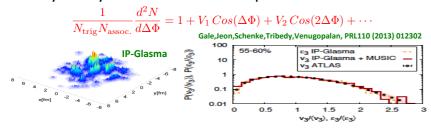
Raju Venugopalan

Probing extreme QCD through ridge-like correlations in small systems: status and problems

The ridge in A+A collisions

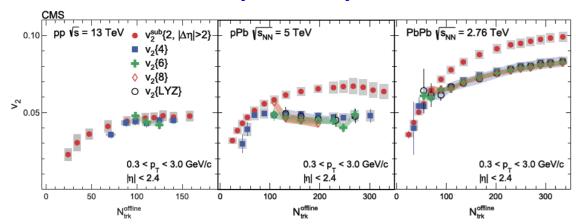


Structure of ridge-correlations can be understood as hydrodynamic flow driven by event-by-event fluctuations in nucleon positions

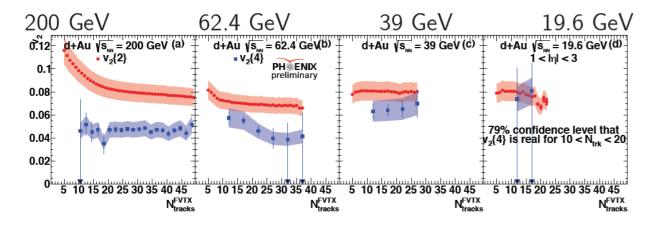


Some evidence of sensitivity of data to sub-nucleon scale fluctuations

Collectivity across system size

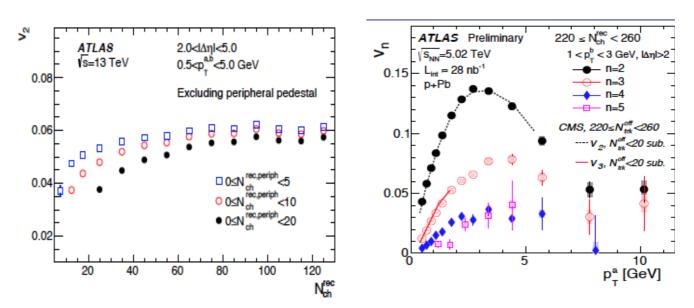


Collectivity across wide energy scales



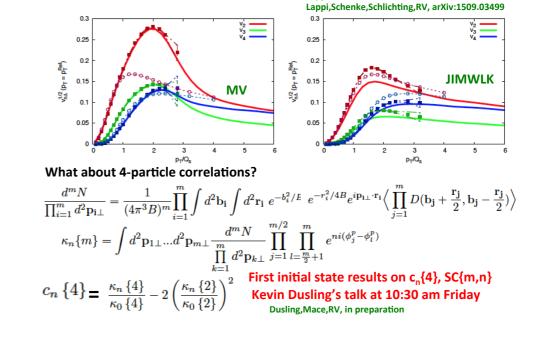
Strong final state interactions? Hydrodynamics fits to the data, but correlations are observed up to high transverse momenta and small multiplicity.

Issues with the hydrodynamic paradigm: III



Tracing azimuthal initial state correlations

Lappi, arXiv:1501.05505



Kevin Dusling

Collectivity from the initial state: Four-particle correlations in proton-nucleus collisions

Collectivity from four-particle initial state correlations has remained elusive...

Compute v₂{m} systematically for the first time in an initial state framework

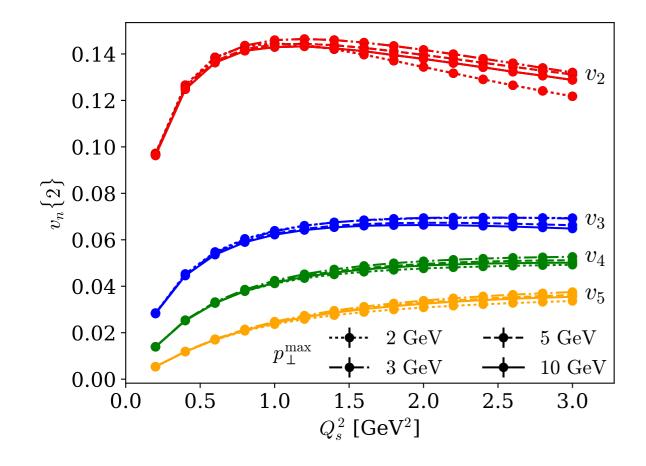
First computation of the average of the product of four light-like "dipole" Wilson-line correlators

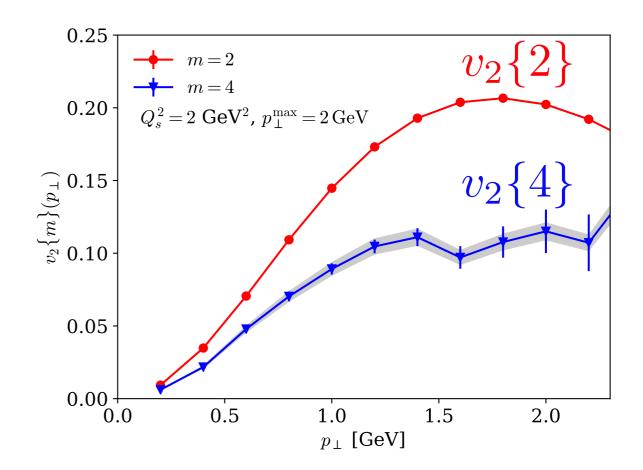
$$W_q(\mathbf{b_i}, \mathbf{k_{i\perp}}) = \frac{1}{\pi^2} e^{-|\mathbf{b_i}|^2/B} e^{-|\mathbf{k_i}|^2 B}$$

Quark distribution

$$\frac{d^m N}{d^2 \mathbf{p}_{\mathbf{i}\perp} \cdots d^2 \mathbf{p}_{\mathbf{m}\perp}} = \prod_{i=1}^m \int d^2 \mathbf{b_i} \int \frac{d^2 \mathbf{k_i}}{(2\pi)^2} W_q(\mathbf{b_i}, \mathbf{k_{i\perp}})$$

$$\cdot \int d^2 \mathbf{r_i} e^{i(\mathbf{p_{i\perp}} - \mathbf{k_{i\perp}}) \cdot \mathbf{r_i}} \left\langle \prod_{j=1}^m D\left(\mathbf{b_j} + \frac{\mathbf{r_j}}{2}, \mathbf{b_j} - \frac{\mathbf{r_j}}{2}\right) \right\rangle.$$





1/Qs 1/Qs

Long-range collectivity via subevent cumulants

Summary of collectivity in small system

■ Collectivity associated with ridge must involve many particles in multiple η ranges → access via subevent cumulant methods

Challenge for both initial & final state scenarios?

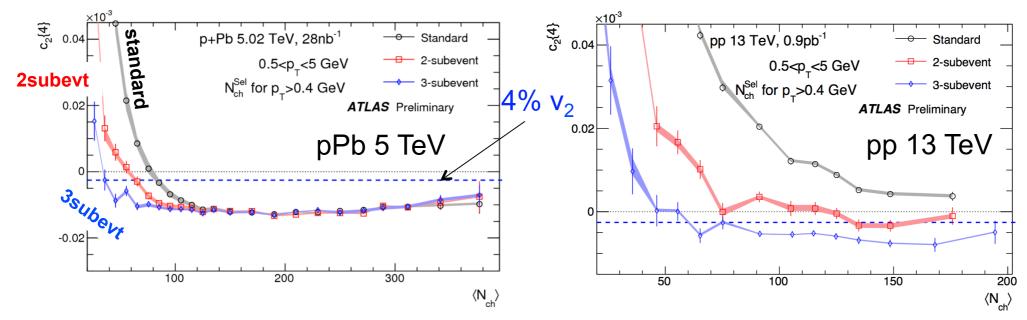
- LHC v_2 associated with ridge does not turn off at low N_{ch} .
- RHIC $v_2\{4\}$ increases and approach $v_2\{2\}$ at lower \sqrt{s}

Challenge (or not) for initial state only scenarios?

- LHC $v_2^{pp} < v_2^{pPb}$ in all N_{ch} and all \sqrt{s} .
- LHC $c_2\{4\}$ <0 down to very low N_{ch} and more negative at higher p_T .
- RHIC geometry scan suggest ordering of v_n follows that of ε_n .
- LHC 5% v_2 at $p_T \sim 10$ GeV.
- LHC symmetric cumulants SC(2,3), SC(2,4) similar to PbPb

Coexistence of initial state & final state scenarios?

Key issue: How to constrain timescales for onset of collectivity?

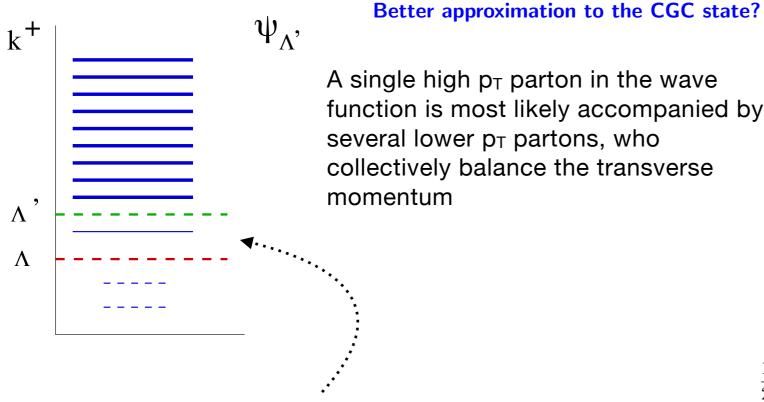


arXiv:1701.03830

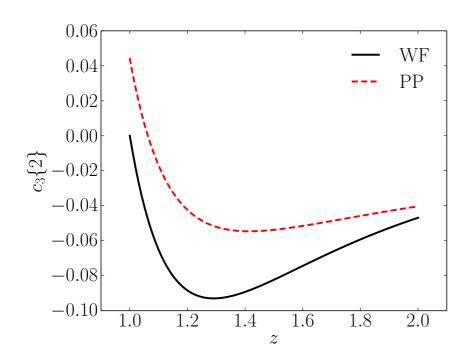
pPb: methods consistent for N_{ch}>100, but split below that

Alex Kovner

Exploring correlations in the CGC wave function

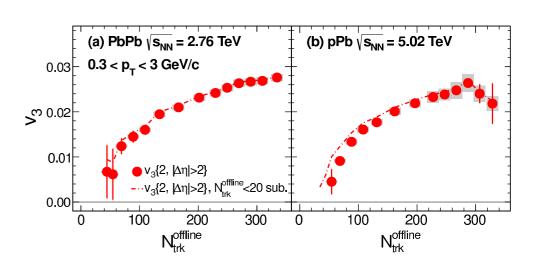


The reproduce v₃ one should take into account correlations of soft gluons



third cumulants

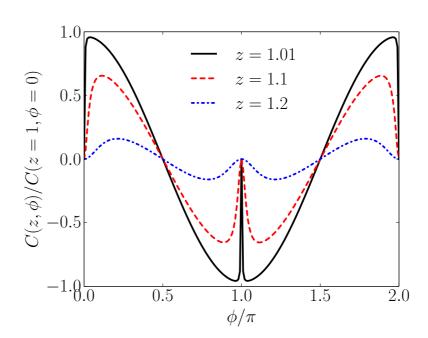
Study correlated structure of the initial wave function



double inclusive spectrum

$$\frac{1}{2} \frac{\frac{d^6 N}{d^2 k d^2 p d \eta_k d \eta_p}(k, p) - \frac{d^6 N}{d^2 k d^2 p d \eta_k d \eta_p}(k, -p)}{\frac{N_c^4 S_{\perp}^2 \mu^4 \lambda^4}{k^4 p^4}} = \frac{\alpha_s N_c}{S_{\perp} p^2} C(z = p/k, \phi)$$

correlation function

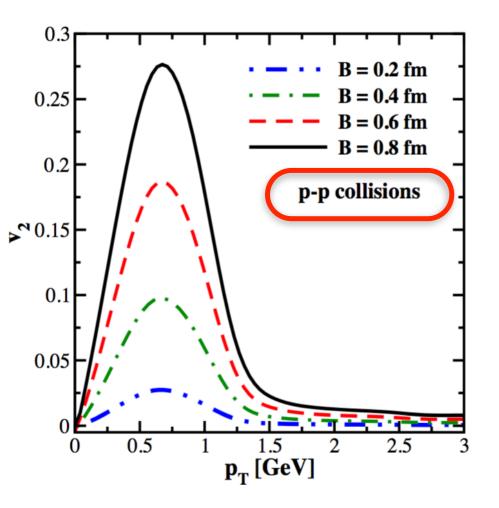


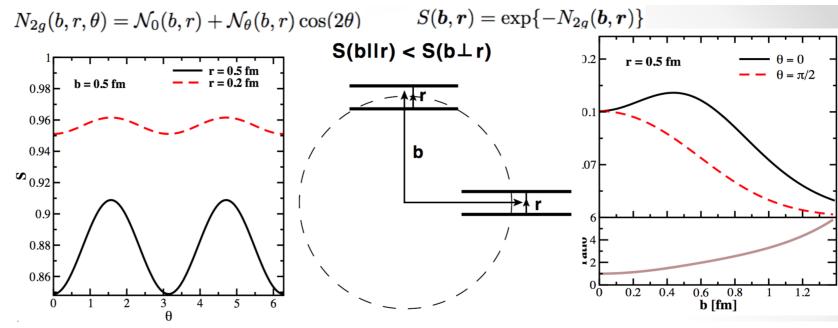
A. Kovner, M. Lublinsky and V. Skokov, arXiv:1612.07790 [hep-ph]

Amir Rezaeian

Elliptic flow from color-dipole orientation in pp and pA collisions

Color dipole orientation as an origin of elliptic flow



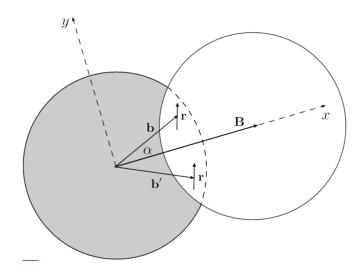


The scattering is stronger when the dipole orientation is (anti)parallel to its impact parameter $(\theta = 0 \text{ or } \theta = \pi)$ than for a dipole perpendicular on b $(\theta = \pi/2)$.

♦ The difference between 'parallel' and 'perpendicular' scattering increases with the dipole size **r** and also with the impact parameter **b**.

$$v_{2}(p,b) = -\frac{\int r dr e^{-\mathcal{N}_{0}(b,r)} J_{2}(pr) \int d\theta e^{-\mathcal{N}_{\theta}(b,r) \cos(2\theta)} \cos(2\theta)}{\int r dr e^{-\mathcal{N}_{0}(b,r)} J_{0}(pr) \int d\theta e^{-\mathcal{N}_{\theta}(b,r) \cos(2\theta)}}$$
$$= \frac{\int r dr e^{-\mathcal{N}_{0}(b,r)} J_{2}(pr) I_{1} (\mathcal{N}_{\theta}(b,r))}{\int r dr e^{-\mathcal{N}_{0}(b,r)} J_{0}(pr) I_{0} (\mathcal{N}_{\theta}(b,r))},$$

$$N(\mathbf{b}||\mathbf{r}) > \mathbf{N}(\mathbf{b} \perp \mathbf{r})$$
 $-\mathcal{N}_{\theta} > 0 \longrightarrow v_2 > 0$



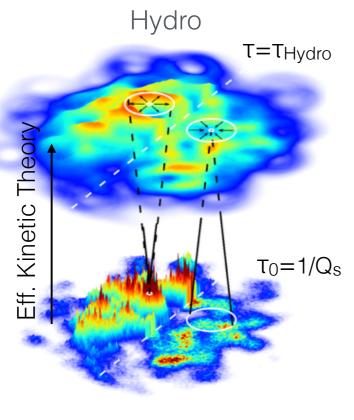
E. Iancu and A. Rezaeian, arXiv:1702.03943

Sören Schlichting

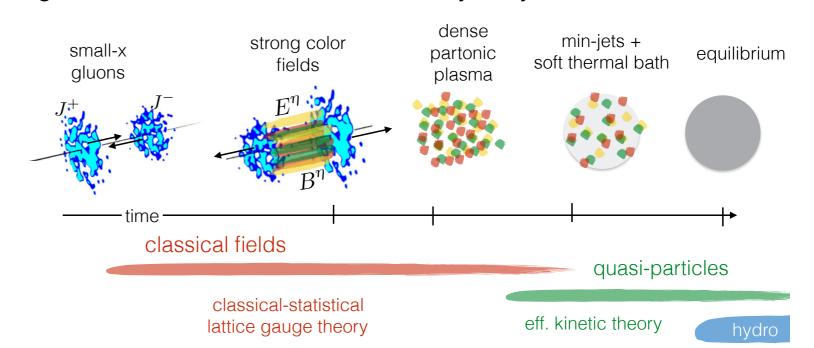
Event-by-event pre-equilibrium dynamics — from gluon saturation towards the onset of hydrodynamics

Extract energy-momentum tensor $T^{\mu\nu}(x)$ from classical statistical lattice simulation

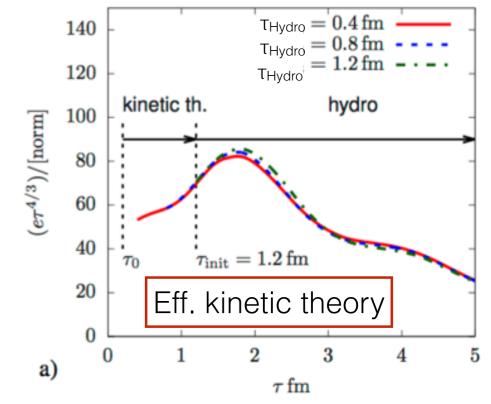
Evolve $T^{\mu\nu}$ from initial time $\tau_0 \sim 1/Q_s$ to hydro initialization time τ_{Hydro} using eff. kinetic theory description



class. Yang-Mills



 $T^{\mu\nu}(\tau,x) = T^{\mu\nu}_{BG}\Big(Q_s(x)\tau\Big) + \int_{Disc} G^{\mu\nu}_{\alpha\beta}\Big(\tau,\tau_0,x,x_0,Q_s(x)\Big) \,\delta T^{\alpha\beta}(\tau_0,x_0)$



energy-momentum tensor

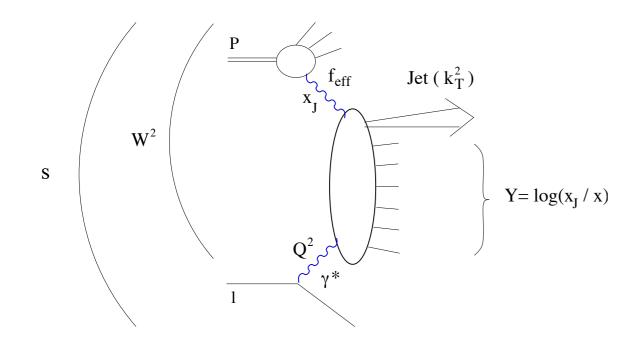
A. Kurkela, A. Mazeliauskas, J.-F. Paquet, S. Schlichting, D. Teaney (arXiv:1704.05242)

Energy density in the central

region of Pb+Pb collision

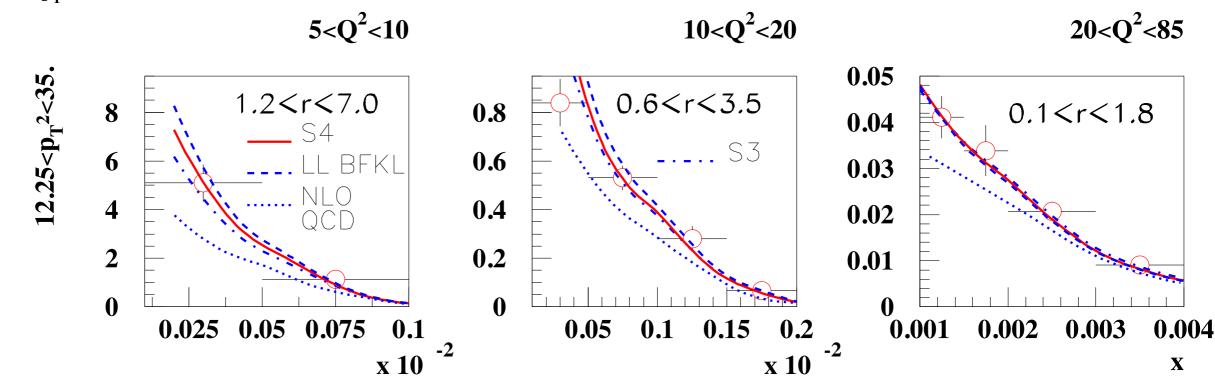
Christophe Royon

Probing the BFKL dynamics at hadronic colliders



- Full implementation of BFKL NLL kernel for many jet proceeses at HERA, Tevatron and LHC
- Forward jets at HERA: DGLAP NLO fails to describe HERA data, good description of data using BFKL NLL formalism
- Mueller Navelet jets: Larger decorrelation expected for BFKL formalism, unfortunately suffers a lot of higher order corrections, NLL BFKL with saturation in progress
- Jet veto measurements in ATLAS: mainly not related to BFKL resummation effects
- Jet gap jets:
- NLL BFKL cross section implemented in HERWIG (Kernel)
- Fair description of D0 and CDF data
- Full NLL calculation in progress
- Jet gap jet events in diffraction: clean tests of BFKL, modulo the survival probability (and its depndence on kinematics)

 $d \sigma/dx dp_T^2 d Q^2 - H1 DATA$



Akio Ogawa

Polarized p+A Physics at Forward Rapidity at STAR

- STAR @ RHIC can reach the saturation region at forward rapidity in p+A
- Polarized protons
- Scanning A → Au, Al, ...
- p_T scan and rapidity/x scan may allow to cross saturation scale Q_s^2 (x)

STAR can study evolution of $Q_s^2(x)$ with A



- Small to no suppression in p+Au
- Results coming soon for
 - Di-hadron angular correlation
 - R_{DA} for π^0 and photons

RHIC 2015

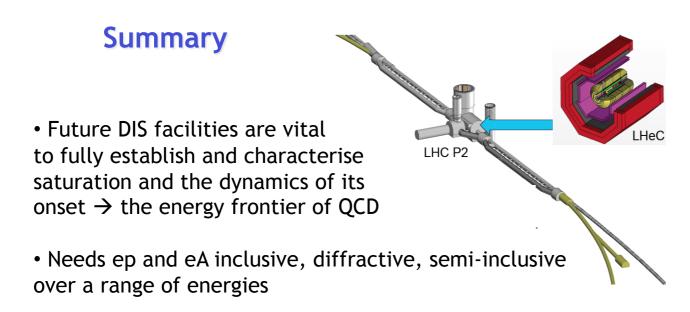
- $\vec{p} + p$, $L_{\text{int}} = 40 + 50 \text{ pb}^{-1}$
- $\vec{p} + Al$, $L_{\text{int}} = 1.0 \text{ pb}^{-1}$
- $\vec{p} + Au$, $L_{\text{int}} = 0.45 \text{ pb}^{-1}$

 Future forward upgrade at STAR is proposed, including saturation/pA physics at forward and

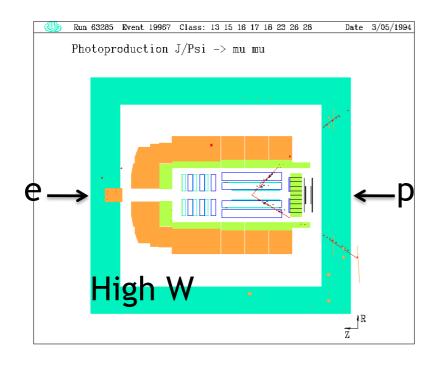
STARIDATE THE OFFICE STARIDATE OF STUDY LOW-X

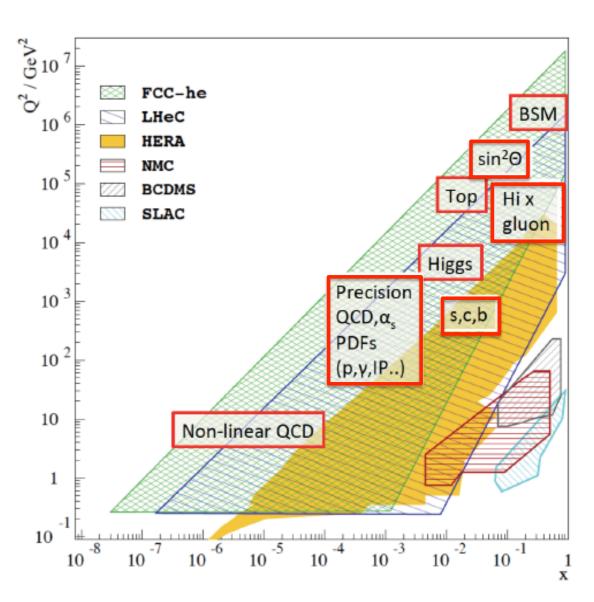
Paul Newman

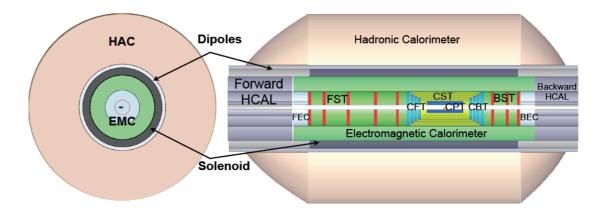
Low x physics and saturation: from HERA to future DIS and the LHeC



- Complementarity beween EIC and LHeC
- LHeC working towards next CERN Council European Strategy exercise (2020) with a view to running in later stages of LHC (post-LS4, from ~2031) ... lots to do!

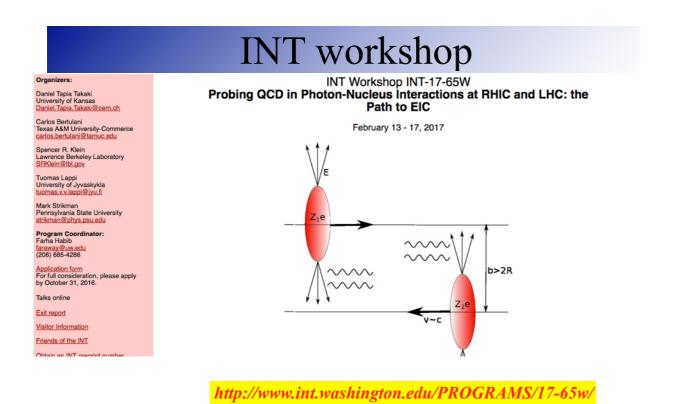




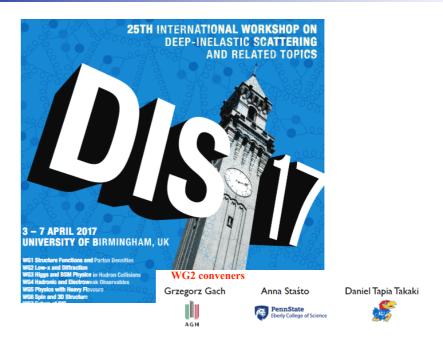


Daniel Tapia Takaki

Studying gluon saturation and nuclear gluon effects using forward heavy-ion probes and UPCs



DIS 2017



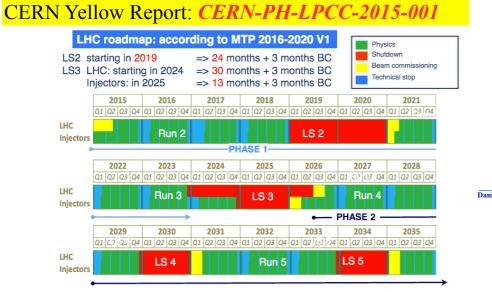
Daniel Tapia Takaki Saturation: Recent developments, new measurements/ideas – BNL April 26 2017

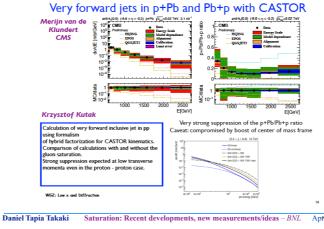
Daniel Tapia Takaki

Daniel Tapia Takaki

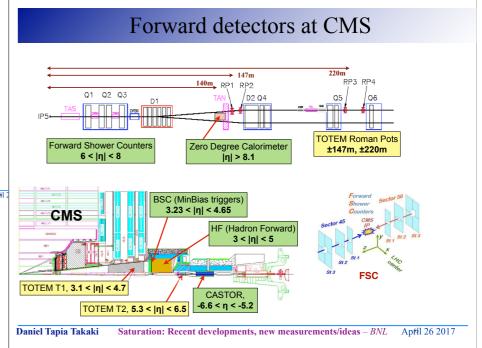
Saturation: Recent developments, new measurements/ideas – BNL April 26 2017

possible to use CASTOR in UPC studies in the future LHC schedule





From DIS 2017 —sensitive to saturation ... Not UPCs but



Saturation: Recent developments, new measurements/ideas – BNL April 26 2017

BNL-113876-2017

RIKEN/RBRC Workshop Saturation: Recent Developments, New Ideas and Measurements April 26-28, 2017

Tuomas Lappi (U. Jyvaskyla) Vladimir Skokov (RBRC) Andrey Tarasov (BNL) Thomas Ullrich (BNL/Yale U)

Proceedings of RIKEN BNL Research Center Workshop

Volume 129



- Small x evolution and hadron production at NLO
- · Spin at small x
- TMD physics
- Small-x physics in e+p and e+A DIS
- · Particle production in pA
- Correlations

27 Presentations in 3 days

I. Balitsky
G. BeufFull NLO corrections for DIS structure functions in the dipole factorization formalism
S. Caron-HuotLinear and nonlinear small-x evolution in perturbation theory
S. Caron-HuotNuclear Theory/RIKEN Seminar: Analyticity in Spin and Causality in Conformal Theories
G. Chirilli
A. DumitruFluctuations of the gluon distribution at small-x: correlation of multiplicity and transverse momentum fluctuations
K. Dusling
K. FukushimaParticle production in CGC
E. IancuParticle production in proton-nucleus collisions beyond leading order
J. JiaFlow in small systems
D. KharzeevDeep inelastic scattering as a probe of entanglement
Y. KovchegovSmall-x asymptotics of the quark helicity distribution
A. KovnerExploring correlations in the CGC wave function: odd azimuthal anisotropy
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